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On the simulation of streamflow using hybrid tree-based machine learning models: A case study of Kurkursar basin, Iran --Manuscript Draft--

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Full Title:	On the simulation of streamflow using hybrid tree-based machine learning models: A case study of Kurkursar basin, Iran
Article Type:	Original Paper
Abstract:	<p>The most important concern of hydrologists in the analysis of water resources for planning and managing sustainable water resources is the reliable and accurate prediction of streamflow. In this regard, the application of data mining algorithms has grown significantly in recent decades. In the present study, seven standalone decision tree models, namely Random Forest (RF), Random Tree (RT), REP Tree (REPT), instance-based learning (IBK), KStar, M5P, and Bagging, and six hybrid models, namely Random Sub Space-REP Tree (RS-REPT), Random Sub Space-Random Tree (RS-RT), Random SubSpace-M5P (RS-M5P), Random Committee-REP Tree (RC-REPT), and Random Committee-Random Tree (RC-RT), were used to predict streamflow in the Kurkursar River, Iran. A time series from 1989 to 2019 was used for training (8%) and testing (20%) phases. The RMSE, PSR, MAE, PBIAS, and NSE statistical criteria were employed to evaluate the performance and accuracy of the models, and dimensional diagrams were drawn to assess them visually. The results showed that among all the standalone and hybrid models, BAGGING had the best performance (RMSE=0.51615 $[[EQUATION]]$, MAE=0.09201 $[[EQUATION]]$, NSE=0.7467, PBIAS=-10.511%, and PSR=0.50319) and the REP Tree (REPT) model the weakest performance (RMSE= 1.36649, MAE= 0.2451607, NSE= 0.3327, PBIAS - 11.274, and PSR= 0.81685). The research results generally show that standalone and hybrid models performed very well. It can also be deduced that the performance of standalone and hybrid models are very close to each other, and there is no significant superiority between single and hybrid models.</p>

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7 2 **models: A case study of Kurkursar basin, Iran**
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4 **19 Abstract**
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23 28 River, Iran. A time series from 1989 to 2019 was used for training (8%) and testing (20%) phases.
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27 30 performance and accuracy of the models, and dimensional diagrams were drawn to assess them
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31 32 best performance (RMSE=0.51615 $\frac{m^3}{s}$, MAE=0.09201 $\frac{m^3}{s}$, NSE=0.7467, PBIAS=-10.511%, and
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33 33 PSR=0.50319) and the REP Tree (REPT) model the weakest performance (RMSE= 1.36649,
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35 34 MAE= 0.2451607, NSE= 0.3327, PBIAS -11.274, and PSR= 0.81685). The research results
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37 35 generally show that standalone and hybrid models performed very well. **It can also be deduced that**
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41 37 **significant superiority between single and hybrid models.**

42 **38 Keywords:** Data mining, Hybrid model, Kurkursar river, Streamflow prediction
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1. Introduction

Streamflow prediction for watershed planning and management, drought risk assessment, and water resource development has become vital and challenging for engineers and hydrologists (Steinfeld et al., 2015). However, the complex nature of processes such as streamflow makes their accurate prediction difficult. At the moment, there are several hydrological methods for simulating the streamflow process, including physical, conceptual, experimental, Artificial Intelligence (AI), and Data Mining (DM) models (Jothiprakash & Magar, 2009; C. L. Wu & Chau, 2011).

Today, the growth of technology has increased so much that it has changed the direction of our lives, and, in this regard, AI, which is a relatively new trend in science, has brought about fundamental changes. As a part of artificial intelligence, machine learning and data mining models are structured to employ fundamental relationships in data for prediction in different areas by modeling (Moosavi et al., 2020). The main purpose of machine learning is to design and develop intelligent applications that can access data and use them in the learning process (Travassos et al., 2020).

Many companies and organizations around the world need new techniques and tools, including machine learning and data mining, to achieve their ideals and fundamentals in dealing with the new challenges of today’s ever-evolving world (Dogan & Birant, 2020). In the field of engineering, to identify and solve problems, the testing process is divided into three models: White, Black, and Gray Boxes. The Black Box model does not pay attention to the internal mechanism of a system or a tool and focuses only on the output produced based on the selected input for the operating conditions (Henzinger et al., 2006). In the White Box model, the internal mechanism of a system is also tested (Korel, 1990). Finally, in the Gray Box modeling, the model structure is derived from physical principles by evaluating the parameters through experimental data (Bäumelt



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4 67 & Dostál, 2020). Currently, there are several hydrological models to simulate this process (C. L.
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6 68 Wu & Chau, 2011), which can be categorized as physical, conceptual, experimental, and artificial
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9 69 intelligence (AI) models (Jothiprakash & Magar, 2009). Streamflow prediction using artificial
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11 70 intelligence techniques can be classified into four classes of data-based regression classification,
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13 71 evolutionary computation, fuzzy sets, and combined (with other models) (Cigizoglu, 2005; Yaseen
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15 72 et al., 2015). From another perspective, these models can be divided into experimental (black box),
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17 73 conceptual (gray box), and physical (white box) models (Worden et al., 2007). The black box
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19 74 (experimental) model is developed without considering the physical processes associated with the
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21 75 watershed. They only operate based on simultaneous input and output time series analysis (Azodi
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23 76 et al., 2020). Conceptual models or gray boxes are based on physical laws and can describe
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25 77 hydrological behavior by empirical expression. Gray box models require less data than physical
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27 78 models and, thanks to the calibration process, demand less computational volume and time
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29 79 (Salcedo-Sanz et al., 2016). Black box does not use physical process information, and its main
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31 80 focus in the modeling process is solely on data. Therefore, it can be said that in the black-box
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33 81 model, the input has a different structure for the forecasting process (Dastorani et al., 2010; Mehr
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35 82 et al., 2015). These models make decisions based on previously stored data and reduce the
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37 83 likelihood of error, hence solving the most complex and difficult problems very quickly without
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39 84 the slightest mistake.

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48 85 AI models have many advantages in science, especially by reducing repetitive processes
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50 86 and not requiring complex equations (Afan et al., 2015; Deo & Şahin, 2016; Shu & Burn, 2004).
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52 87 ANNs have a special place among AI models. Such models have been increasing due to various
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54 88 merits such as accuracy, convergence speed, and volume of calculations (Pradhan et al., 2020).
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56 89 One of the main advantages of ANNs is that they do not need comprehensive information on the
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90 physics of the problem. They also have a very high capability to use incomplete data. Another
91 advantage is that when we have missing data, using these models seems very reasonable (Minns
92 & Hall, 1996). ANNs can be used in different fields of hydrological modeling, e.g., for rainfall-
93 runoff (Adnan et al., 2020; Alizadeh et al., 2020; Kassem et al., 2020; Parisouj et al., 2020; Snieder
94 et al., 2020), sediment (Asheghi & Hosseini, 2020; Banadkooki et al., 2020; Ebtehaj et al., 2020;
95 Ehteram et al., 2020; Meshram et al., 2020; Seo et al., 2020), flood (Cheng et al., 2020; Dtissibe
96 et al., 2020; Kumar & Yadav, n.d.; Kurian et al., 2020; Luu et al., 2020; Obasi et al., 2020), and
97 evapotranspiration (Guan et al., 2020; Malik et al., 2020; Mohamadi et al., 2020; Seifi & Soroush,
98 2020; L. Wu et al., 2020).

99 However, there are some drawbacks with the ANNs, and the main issue is finding the
100 optimal values (solution) for weight and bias coefficients (Bashir & El-Hawary, 2009). To
101 overcome this problem, optimization algorithms (metaheuristics) are commonly used to optimize
102 the coefficients. Metaheuristic models use mathematical programming to determine the optimal
103 value of one or more objective functions and include randomly structured search elements that
104 follow empirical instructions; they are often inspired by observations of natural phenomena
105 (McKinney & Lin, 1994; Nicklow et al., 2010). These algorithms examine many factors such as
106 time and speed of convergence and identify how to reach the optimal global solutions. Further
107 research should be conducted to investigate strategies for exiting local optimal solutions and those
108 for increasing the accuracy and efficiency of such models. These algorithms can be applied with
109 small modifications to various optimization problems, hence a significant improvement in finding
110 high-quality solutions to difficult optimization problems. A common feature of such algorithms is
111 local optimization exit mechanisms.

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4 112 In this research, we use tree-based models to predict streamflow. Decision tree models can
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7 113 be applied to various fields. Random forest is a common decision tree model with applicability to
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9 114 various areas such as streamflow prediction (Abbasi et al., 2020; Araza et al., 2020; Pham et al.,
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11 115 2020; Zeng et al., 2021), flood forecasting (Kim & Kim, 2020; Pahlavan-Rad et al., 2020; Schoppa
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13 116 et al., 2020; Vafakhah et al., 2020), evapotranspiration (H. Chen et al., 2020; Granata et al., 2020;
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15 117 Karimi et al., 2020; Saggi & Jain, 2020; Salam & Islam, 2020), groundwater prediction (Avand et
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17 118 al., 2020; W. Chen, Li, Tsangaratos, et al., 2020; Lahjouj et al., 2020; Norouzi & Moghaddam,
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19 119 2020; Sachdeva & Kumar, 2020), etc. In the present paper, daily data were utilized to predict
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21 120 streamflow. The variables used included precipitation (R) and discharge (Q). The models were of
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23 121 two categories, standalone and hybrid. The main purpose of this study was to predict the
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25 122 streamflow of the Kurkursar river in Iran via data mining algorithms. Moreover, we intended to
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27 123 evaluate the performance of hybrid models compared to standalone models to determine whether
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29 124 hybrid models would lead to more accurate results. In this study, we seek to compare the
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31 125 performance of single and hybrid models based on decision trees and measure the factors effective
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33 126 on the optimal selection of results to select the best combination for each model and their internal
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35 127 factors based on the physics of the problem is optimized. In this regard, the model composition is
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37 128 determined based on correlation, and the internal factors and parameters of the model will be
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39 129 optimized. We will also try to make a comparison between single and hybrid models and further
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41 130 evaluate their advantages and disadvantages. Finally, the research will be summarized and the
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43 131 success factors in modeling will be addressed and practical suggestions will be provided to
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45 132 increase the research efficiency.
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59 134 **2. Materials and Methods**
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2.1. Case Study

A catchment is a part of the land where the whole water that has fallen or flowed reaches an endpoint. As we know, Iran is a country located in West Asia. It is the second-largest country in the Middle East. The main catchments of the country include the Caspian Sea, the Persian Gulf and the Sea of Oman, Lake Urmia, the Central Plateau, the Eastern Plateau, and Qaraqom (Sarakhs). The Central Plateau basin has the **widest**, and the Sarakhs basin has the **lowest** area. closed or inland basins constitute about 4.73% of the country's area. The Caspian Sea catchment area includes the sub-basins of Aras, Sefidrood, Kurkursar, Lahijan, Haraz, Atrak, and Qarasu. The study area of this research is the Kurkursar basin in Nowshahr city, Mazandaran province, in Northern Iran, with an area of about 75 km². In terms of hydrological classification, it is considered as one of the Caspian sub-basins located between the longitudes 51°23'28" and 51°29'33" East and latitudes 33°36'39" and 36°29'48" North. The average elevation of the Kurkursar watershed is 890 meters, and, according to studies, the slope of the Kurkursar basin is 12.3 degrees in the direction of 111 degrees East. Figure (1) shows the geographical location of the area.


[Fig 1]


2.2. Algorithms and Models

Decision trees are a new and advanced generation of data mining models that have extensively been developed in recent decades. These techniques can discover and extract knowledge from a database and create prediction models (Kazeminezhad et al., 2005). They are now among the most well-known data mining methods and tools for classification and prediction, which, unlike neural networks, generate laws. The decision trees explain their prediction in the

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4 157 form of a set of rules. This research uses eight standalone (RF, RC, RT, REPT, IBK, KStar, M5P,
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6 158 Bagging) and six hybrid models (RS-REPT, RS-RT, RS-M5P, RC-REPT, RC-RT, and RC-RF)
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9 159 based on decision trees.

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15 161 2.2.1 **M5P** 

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18 163 As well known, the M5P algorithm (Wang & Witten, 1996) is, in fact, an extended version
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21 164 of M5, which was discovered and developed by Quinlan (1992). Although there are many learning
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23 165 assembly models, there is no doubt that decision tree models have a special place among them.
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25 166 These models have precise performance and are **known to be very cheap**. Moreover, **They** show 
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27 167 very good performance in terms of regression (Nhu et al., 2020). Another main advantage of
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29 168 decision trees is their quite desirable performance when very large data is in hand with high
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31 169 features and dimensions. Even when there is a great amount of missing data in a project, such
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33 170 models have high technical justification (Behnood et al., 2017). The decision trees create a tree-
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35 171 like structure for prediction by starting with all the instructional examples, selecting the variable
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37 172 that best categorizes them, and forming subcategories. Tree branches result from an experiment
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39 173 performed by the algorithm with intermediate nodes at each stage. Predictions also appear in the
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41 174 tree leaves (Debeljak & Džeroski, 2011). The M5P tree model can numerically predict continuous
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43 175 variables from numerical traits, and the predicted results appear as multivariate linear regression
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45 176 models in the tree leaves (Frank et al., 1998; Wang & Witten, 1996). The division criterion is based
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47 177 on selecting the standard deviation (SDR) of the output values that reach the node as a measure of
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49 178 error. The expected reduction in error is calculated by testing each attribute (parameter) in the
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$$SDR = \frac{\xi}{|\psi|} \times \beta(i) \times \left[sd(\psi) - \sum_{k \in (L,R)} \frac{\psi_K}{|\psi|} \times sd(\psi_K) \right] = sd(\psi) - \sum_k \frac{\psi_K}{|\psi|} \times sd(\psi_K) \quad (1)$$

Where SDR is the standard deviation reduction, ψ represents the series of instances that reach the node, m indicates the number of instances that do not have missing values for this attribute, $\beta(i)$ is a corrective factor, and L and R are sets that arise from the division of this attribute.

2.2.2. Random Forest (RF)

Random forest is one of the well-known and widely used algorithms in soft computing and data mining (Breiman, 2001; Chernick, 2002). Using this model is very simple and leads to high accuracy in forecasting with generally desirable results. This algorithm is also applicable to multiclassification and regression (de Santana et al., 2018; Quiroz et al., 2018) since it has a relatively low sensitivity to multicollinearity. This model achieves excellent results with missing and unbalanced data (W. Chen, Li, Xue, et al., 2020; Tsagkrasoulis & Montana, 2018). Each tree branch is identified using a random subset of variables/factors in each node during the RF modeling process. The final result of the modeling process is the average of all the trees (Cutler et al., 2007). To implement the stochastic forest model, it is necessary to define two basic parameters, namely the number of variables (factors) used in each stage of the tree building process (m_{tree}) and the number of trees to be built in the forest (n_{tree}). In order to minimize the generalization error, the mentioned parameters must be optimized (Liaw & Wiener, 2002). Some researchers (e.g., Bryman, 2001; Liaw and Wiener, 2002) have stated in their studies that even one variable ($m = 1$) can be accurate, while others (e.g., Grömping, 2009) consider at least two variables to be necessary. However, in order to avoid using weaker regressions as a separator, it is better to assume

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200 (m = 1,2,3, ...). RF is a set of classification and regression (CART) trees calculated from Equation
201 (2):

$$\{\varphi(\tau, \theta_\xi), \xi = 1, 2, \dots, i, \dots\} \tag{2}$$



203 where φ is random forest classification, τ is an input variable, and $\{\theta_\xi\}$ represents
204 independent and distributed random vector variables used to generate each regression and
205 classification tree. The calculation of important variables is based on the mean Gini coefficient
206 reduction and the mean accuracy reduction. The Gini coefficient is an error that can be deduced
207 from Equation (3):

$$Gini \text{ coefficient} = 1 - (1 - \sum_C P^2(c|t)) = \sum_{k=1}^k \widehat{p}_{mk} \times (1 - \widehat{p}_{mk}) \tag{3}$$

209 In the above formula, (\widehat{p}_{mk}) indicates the probability of correct classification, C is the number
210 of classes, t represents a tree node, and P stands for the relative frequency of c. The Gini coefficient
211 results from multiplying the probability of correct and incorrect classifications (Jiang et al., 2020).

212 2.2.3. Reduced Error Pruning Tree (REPT)

213 Decision trees can usually be divided into two types of tree (hierarchical) structure and
214 rules (if-then). If the decision tree is complex, the tree structure and rules may be destroyed (X.
215 Wu & Kumar, 2009). Hence, pruning steps are primarily used for a complex tree to facilitate the
216 interpretation and analysis of results. Furthermore, pruning decision trees is essential in
217 optimization to increase computational efficiency and classification accuracy (Rokach & Maimon,
218 2008). There are two standard pruning methods: pre-pruning (back pruning) and post-pruning
219 (pruning forward). The pruning method comprises two growth and pruning stages, allowing one

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220 to over-fit the data and then prune the grown trees. Post-pruning methods perform better than pre-
221 pruning (Mahmood et al., 2010).

222 Pruning error reduction (REP) is a post-pruning method for decision trees, and the REPT
223 model, as one of the fastest methods of model training, is a combination of REP and decision tree
224 algorithm. It is developed based on a decision/regression tree to reduce variance (Breslow & Aha,
225 1997). In the decision tree algorithm, the size of the tree affects the accuracy of data classification.
226 On the other hand, combining two algorithms reduces the synergy in the structure of a decision
227 tree (Sharafati et al., 2019). Therefore, this complexity in the REPT model is reduced by the REP
228 pruning technique, one of the most popular and well-known pruning methods that can target some
229 branches and leaves of trees without affecting the accuracy and precision of the model (Mahmood
230 et al., 2010). The two main advantages of this method include simplifying the tree without
231 reducing accuracy and avoiding the overfitting problem (Khosravi, Mao, et al., 2018; Khosravi,
232 Pham, et al., 2018). The basic REPT relation is given in Equation (4):

$$233 \text{ Gain ratio } (\eta, \xi) = \frac{\text{Entropy}(\xi) - \sum_{i=1}^n \left| \frac{\xi_i}{\xi} \right| \text{Entropy}(\xi_i)}{-\sum \left| \frac{\xi_i}{\xi} \right| \text{Log}_2 \left| \frac{\xi_i}{\xi} \right|} \quad (4)$$

234 In this regard, the property η belongs to the educational dataset ξ with subsets $\xi_i = 1, 2, 3, \dots, n$.

235 2.2.4. Bagging (BA)

236 Bagging is a machine learning method proposed by Breiman (1996). This algorithm
237 increases classification accuracy by combining the classification of randomly generated training
238 sets. It can reduce the variance of the basic algorithms and adjust the estimation to the expected
239 conclusion to improve the accuracy of a model (Dieu Tien Bui et al., 2016; Peters et al., 2002).
240 Also, this method can eliminate the defects of learning components and improve the predictive

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241 ability of weak learners (Yin, 2020). Moreover, due to its sensitivity to minor changes in the
242 training data, this technique can increase the accuracy of the prediction results (Shirzadi et al.,
243 2018). Bagging is most useful when regression models with high variance and low bias, such as
244 regression trees, are fully grown (Gweon et al., 2020). It creates multiple instances from the same
245 dataset by modifying the bootstrap technique. Several separate trees are created for the same
246 prediction and used to generate a whole prediction. The final prediction of the process can be
247 obtained by voting or averaging for classification and regression problems (Erdal & Karahanoğlu,
248 2016; Ribeiro & dos Santos Coelho, 2020).

249 *2.2.5. Random Committee-REPT (RC-REPT)*

250 Random Committee (RC) is a meta-algorithm that possesses classifiers that can be used at
251 the service of the learning power. In the classification process, predictions are made by estimating
252 the average probability, not by voting. This algorithm is used for classification and regression
253 problems depending on the learner base. It can also be combined with other models to form a
254 hybrid classifier model, which in the present study is developed by tree pruning modifiers
255 generating predictions with a direct average probability (Sharafati et al., 2019). They are used to
256 improve the trainability of the model as well as the model that is combined with it (classifier). By
257 this method, a combination of classifier-based methods can be created. For this purpose, WEKA
258 software is used in which, generally, the whole process is divided into two stages of preprocessing
259 and classification. The processing step involves selecting the attribute. In this study, not all
260 attributes of the dataset are necessary for analysis, which leads to a reduction in dimensions and
261 ensures better performance. The second phase involves using machine learning techniques such as
262 random forests, random committees, and random trees to classify samples through voting
263 (Niranjan et al., 2018).

264 2.2.6. *Random Subspace-REPT (RS-REPT)*

265 Another method for group learning is Random Subspace (RS). Ho (1995) first proposed
266 the RS model as a comprehensive classical algorithm. This model has many similarities with the
267 bagging model. It seeks to diversify learners in sampling the feature space. All model components
268 are constructed with the same training data, but each feature is selected randomly, leading to the
269 group's diversity. For the most part, the number of attributes in all committee components is at the
270 same level. When it comes to classification, a group decides either by a majority vote or by the
271 weight of votes. Regression is simply done with the average output of the components. This
272 method aims to increase the general accuracy of decision-based classifiers without compromising
273 the accuracy of training data, which is one of the major and most common problems of tree-based
274 classification (Ho, 1998). Many studies perform RS in pairs with different classifiers having the
275 training subsets randomly made from the main training subsets, which is the only difference from
276 the Bagging algorithm. In this method, the complications of each sub-classifier in the final
277 prediction are obtained through the combined voting method (Bertoni et al., 2005).

278 2.3. *Evaluation criteria*

279 It is necessary to use evaluation indicators to evaluate a model's prediction performance in
280 any research. Accordingly, in the present study, different statistical criteria are used to assess and
281 compare the performance of the models. These criteria include the coefficient of determination
282 (R^2), root mean square error (RMSE), absolute mean error (MAE), Nash-Sutcliffe efficiency
283 (NSE) coefficient, bias, and the squared ratio of mean squared error to standard deviation (PSR).
284 Table (1) summarizes the results for the above indicators. In addition, the qualitative and
285 quantitative values, as well as their allowable ranges, are specified. "ob" represents the observed
286 values, and "pr" is the calculated or predicted value.

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9 289 2.4. Best input combination
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12 290 Finding the relationship between different variables is a major challenge in this process. It
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15 291 can be simply stated that the preliminary and, at the same time, the most important part in the
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17 292 modeling process is the research to determine the effective factors in the prediction process.
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20 293 Therefore, in the first phase of the research, the effective factors that influence the river discharge
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22 294 are determined, and then, with the help of the **Pearson coefficient**, the effect of each factor is
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25 295 determined. The most important factors in streamflow prediction include temperature, humidity,
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27 296 precipitation, evapotranspiration, pressure, wind direction, and discharge. **However, among these**
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30 297 **factors, only precipitation and discharge have the greatest impact on the forecasting process, and**
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32 298 **the effects of other factors can be ignored.** The time series in this research are on a daily basis for
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34 299 the data from 1989-2019 (80% for training and 20% for testing). Table (2) shows some statistical
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37 300 parameters for the datasets used in the training and testing phases.
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40 301 [Table 2]
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42 302 We determined the correlation between input and output variables with the **CC coefficient**,
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44 303 shown in Table (3). It should be noted that the input variables include $R(t)$, $R(t-1)$, $R(t-2)$, \dots , $R(t-$
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46 304 $6)$, $Q(t)$, $Q(t-2)$, \dots , $Q(t-5)$, and the output variable is Discharge($Q(t)$). Table (4) shows the
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49 305 combinations for the input variables.
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55 307 [Table 3] & [Table 4]
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309 3. Results

310 This research aims to predict the streamflow of the Kurkursar river in Iran. First, the
311 required data should be collected and standardized to this aim. The time series of the research data
312 is on a daily basis for precipitation (rainfall) and discharge. After collecting and arranging the data
313 structure, the Weka program was employed to implement the models developed by the University
314 of Waikato. To this end, the data were entered into the program, and the best combination for each
315 model was determined in two phases of training (80%) and testing (20%). The implemented
316 models used in the present study belong to two categories of standalone and hybrid. However,
317 being developed based on the decision tree is their main common trait. Decision trees are helpful
318 when the volume of data is very high. As fully introduced in the previous sections, six standalone
319 and eight hybrid models were used. Table (5) shows the correlation coefficient values in the two
320 phases of training and testing for the standalone models used to choose the best combination.

321 [Table 5]

322 All the data were evaluated to determine which combination would be the best solution
323 for each model. Finally, for the M5P model, the combination of model 2 led to the best solution
324 (CC=0.9264) in the test phase. Also, for Random Forest, the combination of model 4 (CC=0.953);
325 Random Tree, model 4 (CC=1.3945); REP Tree, model 4 (CC=1.0334); Bagging, model 4
326 (CC=1.0314); IBk, model 4 (CC=1.4402); and Kstar, model 4 (CC=1.3323) was identified.
327 Therefore, for all models (except for the M5P model), the combination of model 4 achieved the
328 best results in the test phase.

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4 329 In the next stage, the value of the coefficient of determination (R^2) was determined, for
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6 330 which the results of the testing phase with the standalone and hybrid models are shown in Table
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9 331 (6). Of note, R^2 is a statistical measure of the data close to the fitted regression line.

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15 333 The results in Table (6) show that based on the R^2 coefficient, the M5P model had the best
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18 334 ($R^2=0.7839$) and the KStar model had the weakest performance ($R^2=0.5228$) among the standalone
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20 335 and RS-M5P ($R^2=0.7613$), and RS-RT ($R^2=0.6584$) had the best and weakest performances,
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23 336 respectively, among the hybrid models.

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26 337 One of the main goals of modeling is to reduce error. In the present paper, RMSE, MAE,
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28 338 PSR, NSE, and PSR indices were used to evaluate the models, which are shown in Table (7).

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31 339 **[Table 7]**

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33 340 Table 7 shows the BA has the lowest error among standalone models
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36 341 (RMSE=0.5161 m^3/sec), and REPT has the highest error (RMSE=1.3664 m^3/sec). Therefore, BA
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38 342 has the best performance, and the REPT model has the weakest performance. Among the hybrid
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41 343 models, RS-M5P has the lowest error and the best performance (RMSE= 0.77176 m^3/sec), and the
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43 344 RS-RT model has the highest error and the weakest performance (RMSE= 0.91089 m^3/sec).

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46 345 To assess the predictive models used in the current study, several visual comparisons were
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49 346 made through different graphical figures including, time-series plots (Figure 2), scatter plots
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51 347 (Figure 3), and error graphs (Figure 4). From those figures, it can be concluded that among the
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54 348 standalone models, the IBK model is the closest to the observational data in predicting the
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56 349 minimum values. In simpler terms, this model better predicts the minimum values. However, the
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58 350 BA model's weakest performance in predicting the minimum values. In addition, if we look at
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351 hybrid models, we will see that the results for predicting minimum values are very close to the
352 observational data. Among these models, the performances of the RS-RT, RS-M5P, and RC-RT
353 models are very close and have almost the same performance. In general, among all the models
354 (both single and hybrid), the M5P model has the best performance, and the K Star model has the
355 weakest performance for the minimum values.

[Figs 2-4]

357 To assess the probabilistic features of predictive models, their box plot diagrams are
358 shown in **Figure (5)**. From the figure, it is evident that the IBK model is the closest to the
359 observational data, and the RC-REPT hybrid model has the weakest performance in the first
360 quarter (Q₁). However, the performances are slightly different with the median data, with the M5P
361 and RF models having the best performance and being closest to the observational data. Notably,
362 the M5P model is slightly better than the RF model. Furthermore, the RC-REPT model has the
363 poorest performance in predicting midpoints than the observational data. **In the third quarter (Q₃),**
364 KStar is the best, and RS-RT is the weakest model. Finally, the RT model can predict the maximum
365 data better, and the K Star model is ranked the lowest.



[Fig 5]

368 The "Bag size percentage" parameter specifies a certain number of samples for each
369 member (classifier) of the group. This parameter is determined by the size of the training set
370 (number of training samples) and by distance, and its value is between 10 and 100. The size of
371 each bag is defined as a percentage of the size of the training set. The number of iterations is a
372 measure to stop the error in Weka. The principle of learning in the network is observed in

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373 iterations. The dataset is injected into the algorithm several times, and the algorithm can detect
374 differences in the training data by increasing or decreasing the network parameters. This value is
375 usually assumed to be 10, while some researchers assume it to be 100. The parameter seed is, in
376 fact, a random number. Once its value is fixed, even a random algorithm will behave definitively,
377 and using the same seed will always lead to the same random numbers. There is no definite
378 criterion for determining this parameter, and its optimal value can be calculated by trial and error.
379 Out-of-bag (OOB) error is used to measure the predictive error of random forests, reinforced
380 decision trees, and other machine learning models using Bootstrap aggregation. The bagging
381 model uses sub-sampling with an alternative property to create training examples for model
382 learning. In the present study, optimal coefficients evaluated automatically were measured. The
383 optimized coefficients were tested by trial and error for each model to improve the prediction
384 results. The best-case scenario for the M5P was when the Batchsize value was 100. In this case,
385 the value of RMSE = 1.273 m³/sec is the best solution. To evaluate the effect of Batchsize with
386 trial and error in the range [5-200], the above parameter is added five units in each step to measure
387 its effects. The study results for the mentioned range show that neither increasing nor decreasing
388 this value reduces the error rate. Therefore, the same initial solution of 100 is chosen as the optimal
389 solution. Assuming that the optimal value of the Batchsize parameter = 100 is constant, we can
390 find the optimal MinnumIstance solution, the value of which is automatically equal to 4. The
391 optimal solution is found by trial and error with [20-1] intervals. The results show that from 1 to
392 4, it does not have any effect on reducing the error. However, for the value of 5, the error rate
393 increases and reaches 1.466. This error remains constant for the values from 5 to 20. Accordingly,
394 the value of 4 is selected as the optimal solution for the above parameter. If the Build Regression
395 Tree parameter is set to False, the error value will be 1.273, but if it is set to True, the error value

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396 will reach 1.7247, which indicates an incremental state. Therefore, the default False state is
397 selected as the optimal model since error reduction is aimed. Moreover, the Debug values and the
398 Do Not Check Capabilities in the false mode lead to the optimal solution. If the value of the
399 Unpruned parameter is set to False, the error value will be 1.273. However, in the True mode, the
400 error reaches 1.2344, which indicates a reduction in the amount of error. Therefore, the optimal
401 solution will be in the True mode. If the value of the above parameter is set to False, the error value
402 will be 1.273 m³/sec. But if the above parameter is set to True, the error reaches 0.8181 m³/sec,
403 which indicates a reduction in error. Therefore, the optimal solution is obtained when this
404 parameter is in the True state. Finally, the ultimate solution was the best possible case for the MSP
405 model (Optimized Batchsize=100; MinnumIstance & Num decimal place=4; Build
406 Regression=Tree; Debug=Do Not Check; Capabilities=Save Instances; False, Unpruned & Use
407 Unsmoothed=True). Several trials and errors were carried out to find the optimal coefficients in
408 the RF model. For Bag size percentage, trial and error were performed from 5% to 100%. The
409 results show that by increasing this parameter, the error rate decreases, and the best solution is
410 reached at 100%. Similarly, the trial and error range from 5% to 100% for the Batch size parameter.
411 The results show that increasing or decreasing the value of this parameter does not affect the error
412 rate. Therefore, the same solution of 100% is selected as the optimal one. To calculate the Max
413 Depth parameter, trial and error are performed within the [0-15] interval. The results indicate that
414 the best solution is obtained when its value is equal to zero, and the trend of error from 1 to 15
415 increases. The best solution for the Num Execution Slots parameter is one, and decreasing or
416 increasing its value does not affect the error rate. In the trial and error, this parameter was
417 maintained within the range of [0-10], and it was observed that the error value remained constant
418 without any significant change. The optimal solution was achieved with 100 repetitions, and the

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419 error rate was 0.5466. To find the optimal solution in the [10-200] interval, an error was made after
420 ten repetitions, which was minimized to 40 repetitions. Of note, the error rate up to 60 repetitions
421 had a decreasing trend, but the optimal solution still belonged to repetition 40. For seed parameters,
422 trial and error were performed in two intervals of [0-1] and [0-10]. In the first interval, 0.1 was
423 added in each step to measure the effects, and for the second interval, a unit was added. The optimal
424 state of the model occurred in the first interval, where 0.1 was added. Another result of the trial
425 and error was that increasing the values in the first interval increased the error, but in the second
426 interval, the error remained constant. Increasing this number increased the error rate. Therefore, it
427 can be claimed that increasing the above values causes sensitivity to the error value. There was
428 also a trial and error to optimize the coefficients of the REP Tree model. The best solution for the
429 k value parameter was 1, which reduced the error, while the optimal solution was 0. Increasing
430 this value also increased the error. Increasing the value of the Batchsize parameter did not affect
431 the error. In the trial and error, the range of [5-100] was examined for this parameter. The results
432 showed that the amount of error remained constant within the whole range mentioned; the amount
433 of error did not show sensitivity to Batch size. The best solution for the MaxDepth parameter was
434 zero. The interval [0-100] was considered for trial and error. The amount of error increased at first
435 but decreased significantly over time. The best solution for the MinNum parameter was the default
436 value of zero. In the range of [0-10], trial and error was performed, which showed that the amount
437 of error increased with an increase in the value of this parameter. This increase in error had an
438 upward trend and reached its maximum at the value of 10. Accordingly, the best value for the
439 above parameter was 0.001, with one error occurring within [0-0.01]. In terms of MinVariance
440 Propparameter, error increased with an increase in its value with an upward trend. Accordingly,
441 the error rate was at its lowest level at the zero value for this parameter. For the Num Folds

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442 parameter, the value of zero led to the lowest error and reached the optimal solution. Increasing
443 this parameter also increased the error rate. However, this increase did not have an upward trend
444 and was increasing and decreasing intermittently, with the error gradually getting far from the
445 optimal solution. Finally, the results showed that increasing the Seed parameter had no effect on
446 the error rate, and as the value of this parameter increased, the error rate remained constant.
447 Therefore, number one was chosen as the optimal value. To summarize the above discussion,
448 generally, the program had a good performance. However, to improve the model's performance
449 with all parameters, they should be regulated by trial and error to obtain more optimal values. In
450 general, the results of the forecast were desirable. The optimum values of the parameters used in
451 the predictive models are presented in the Table 8.

[Table 8]

4. Discussion

454 This research aimed to predict streamflow in the Kurkursar catchment in Iran. To this aim,
455 the desired data were collected, which included precipitation and discharge in time series on a
456 daily basis. The correlation coefficient between input and output variables was determined, and
457 different combinations for the model were identified. The models were divided into standalone
458 and hybrid categories. Data were classified into two training and testing classes, and Weka
459 software was used to analyze and evaluate the data.

460 The presented model had a significant effect on reducing variance. It also largely prevented
461 overfitting. Random forests use the bagging algorithm in the learning process, and to reduce
462 overfitting and variance, we created several trees and some data sets in the first step. In the next
463 step, we combined them with the output of the desired model, resulting in which overfitting was

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464 greatly reduced. Generally, the performance meaningfully improves when the missing data are
465 incorporated in the modeling.

466 Random forests have wide applicability in both classification and regression modes, hence
467 their specific position among engineers. However, these models have weaknesses. First of all,
468 many trees are used in random forests, which leads to increased calculations and reduced speed
469 and accuracy of forecasts. Another common problem with these models is that as the number of
470 trees and the output of the model increase, the training period becomes longer. In this case, the
471 model will try to base its final decision on the most votes, prolonging the training process. As for
472 the M5P model, it is based on creating a tree similar to the traditional decision tree (expressed by
473 CART). The specific difference of this model is in its leaves, which generally follow multiple
474 linear regression. It has a relatively good ability to predict various parameters, but its major
475 disadvantage is that changes in data (even small data) may cause instability in the model structure.
476 With an increase in the number of changes, the response time also increases, adding to the
477 complexity of the problem.

478 Moreover, it allocates more time to the training process than other random forest models
479 do, and it faces difficulties when predicting continuous values. However, combining this model
480 with bagging in most cases improves the results and increases the accuracy of prediction. Many
481 researchers have used this combination in predicting hydrological processes and have reported
482 favorable results (Duie Tien Bui et al., 2020; Khosravi, Mao, et al., 2018; Melesse et al., 2020).



483 Another machine learning method used in this article was IBK, which is by nature a lazy
484 learner. It uses linear search algorithms to find the nearest neighbor. The Euclidean distance is also
485 used in this model to evaluate the position of the samples. IBK considers distance from the
486 validation data for weighing estimates of more than one neighbor. Generally, this algorithm has

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4 487 reported good performance in many areas (Angarita-Zapata et al., 2020; Gandhi & Armstrong,
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6 488 2016; Jabbar & Mohammed, 2020; Khosravi et al., 2019; Pattnaik et al., n.d.; Shabani et al., 2020).
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10 489 Moreover, for interpreting the performance of this model, we can say that there is no special
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12 490 training course required. More simply, the learning process occurs when we intend to make real
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14 491 predictions and, in this way, the training data is stored and used. This speeds up reaching the
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16 492 solution. This is while other algorithms (such as vector machines, etc.) devote much more time to
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18 493 the training process, hence their prolonged process to reach the solution. To add to the above
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20 494 advantage, because the algorithm does not need training before prediction, new data will be added
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22 495 seamlessly, ensuring that the algorithm's correct operation is not compromised.
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27 496 Moreover, implementing this algorithm is very easy and fast because it lacks complex and
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29 497 ambiguous parameters. It uses only two parameters, namely the value of K and the distance
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31 498 function. Therefore, it is a very easy algorithm to implement. However, despite all the above, this
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33 499 algorithm also has weaknesses. For example, working with big data in this algorithm is very
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35 500 difficult, and interpretation and analysis in such cases are also unclear. Moreover, with large data,
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37 501 the cost of calculation gets very high. In addition, the distance between the new point and each
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39 502 existing point is very large in this model, which lowers its performance.
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45 503 **5. Conclusion**

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48 504 Four standalone and hybrid models based on the decision tree for rainfall-runoff prediction in the
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50 505 **Korkorsar** watershed in northern Iran were evaluated in the present study. This study aims to use 
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52 506 new decision tree algorithms to predict rainfall-runoff that can be used in other areas of water
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54 507 resources management engineering (such as suspended sediment assessment, flood forecasting,
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56 508 evapotranspiration, etc.). The modeling process indicated **that the factor R (t) is the most important** 
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509 determinant of precipitation-runoff. Other cases of importance included Q (t-1), Q (t-2), R (t-1), Q
510 (t-3), etc., respectively. In this study, it can be inferred that the use of different combinations of
511 variables leads to different levels of performance of the models. The findings showed that
512 predictive accuracy reaches its maximum value (maximum predictive power) when utilized
513 variables with the highest CC.

514 Moreover, the variables with the lowest CC greatly reduced the predictive power of the model.
515 **The results of research modeling show that hybrid models performed better than individual**
516 **models, but it is not possible to comment on their absolute superiority. Therefore, it can be said**
517 **that they may not be equally successful in all cases.**

518 If these models have good and reliable results for a set of data covering a short period, if the period
519 is longer, modeling accuracy will increase accordingly. Research algorithms (based on the decision
520 tree) can be useful for basins with limited measurement networks and fewer.

521 Our results demonstrated that the proposed algorithms could be reliable and cost-effective for
522 predicting hydrological processes in water resources management. **These models are much more**
523 **useful and cost-effective for developing countries where the cost of measuring some hydrological**
524 **parameters is very high.** Of course, these results cannot be generalized to all basins and
525 hydrological processes in absolute terms. But without a doubt, it can be said that algorithms have
526 very high power and accuracy in predicting different hydrological processes.

527 The above models showed acceptable and desirable performance in streamflow prediction.
528 All coefficients were examined by trial and error, and some results were stated in the present
529 article. Standalone models performed well, and while hybrid models were expected to have
530 improved performance, they showed very close results to the former. However, in a qualitative



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531 evaluation of the results, all the models were within a good to good range. Therefore, the following
532 suggestions are made for further research:

- 533 - Use of other tree models and comparison of the results with the present research;
- 534 - Employing the presented models in this study in other hydrological and environmental
535 fields to study their accuracy;
- 536 - Comparison between the models here and other models (such as ANN, SVR, ANFIS,
537 gene expression-Bayesian networks, etc.) in terms of accuracy;
- 538 - Use of other effective factors in streamflow prediction (temperature, humidity,
539 evaporation, transpiration, etc.) in modeling for determining their effects on the
540 efficiency of models;
- 541 - Combining and comparing other different input models;
- 542 - Further evaluation of the rate of delay with the parameters; and
- 543 - A more comprehensive study of the physics of the problem and the structure of the
544 analyzed models. In this regard, their weaknesses can be identified, and necessary
545 measures are taken to strengthen them.

547 **6- Declarations**

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549 **Conflict of Interest:** The authors declare that they have no conflict of interests.

550 **Availability of data and materials :** Please contact the corresponding author for data requests.

551 **Code availability:** Please contact the corresponding author for code requests.

552 **Ethics approval:** Not applicable.

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4 553 **Consent to participate:** Not applicable.

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7 554 **Consent for publication:** Not applicable.

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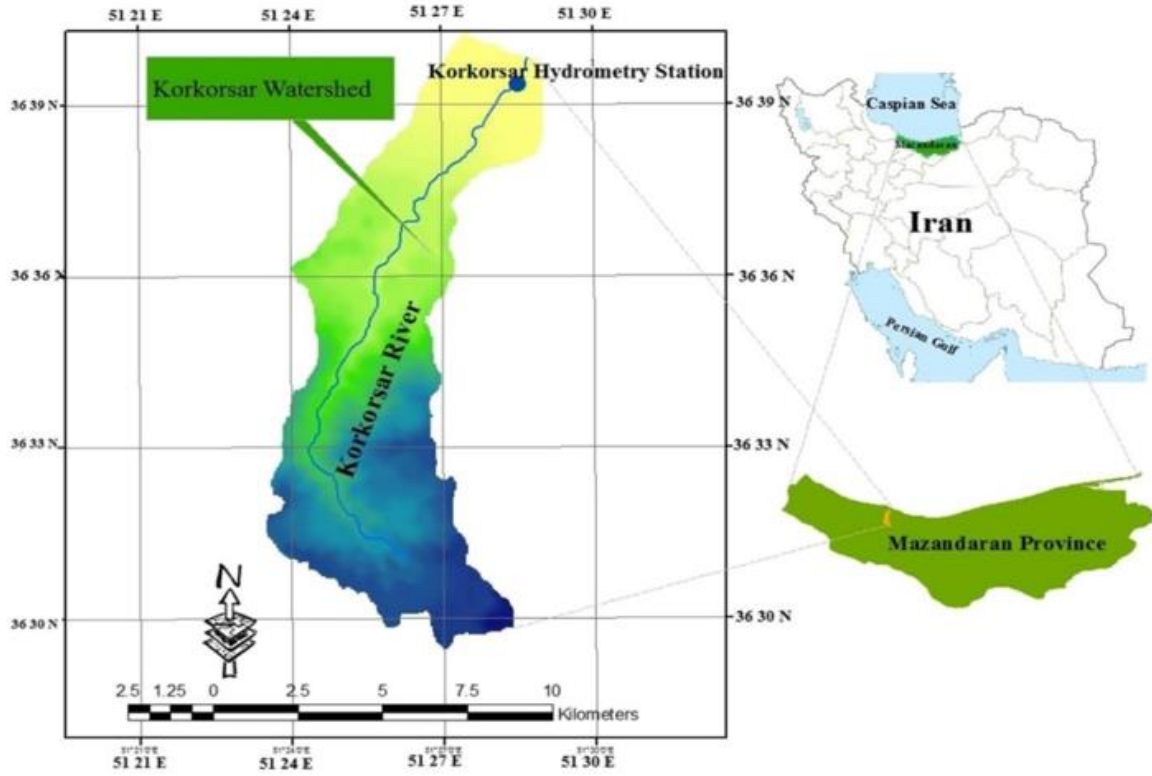
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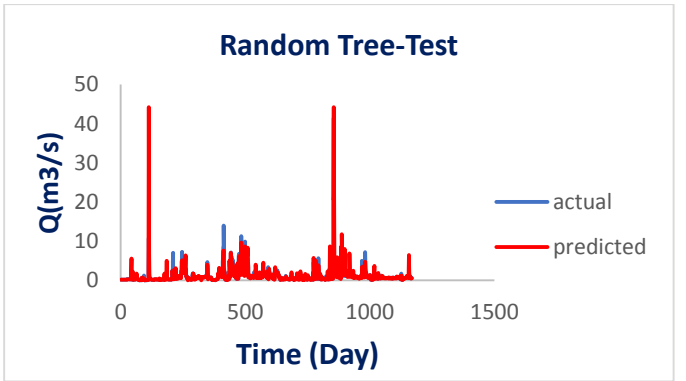
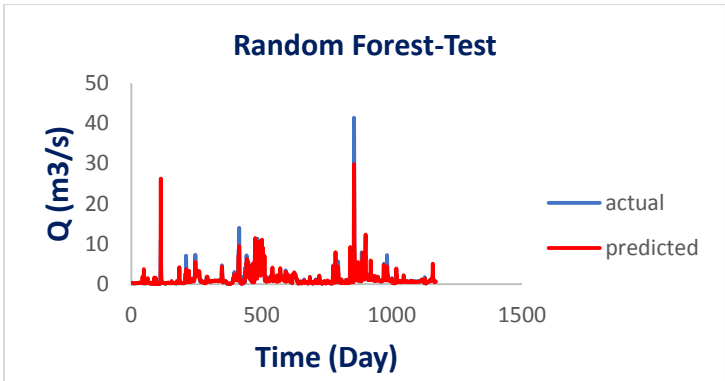
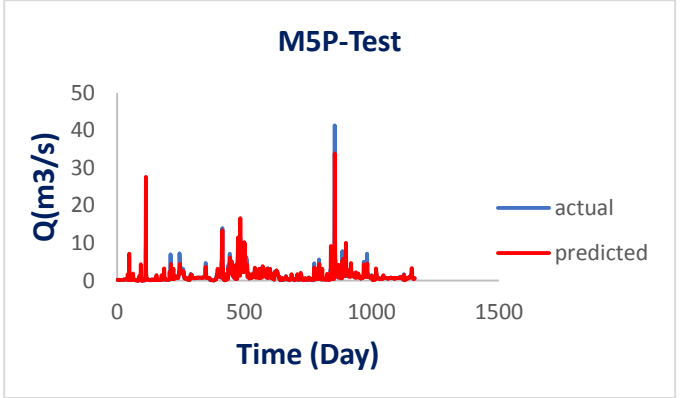
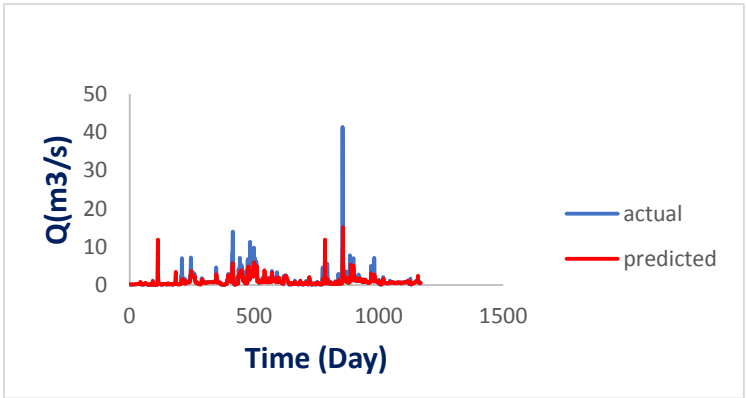
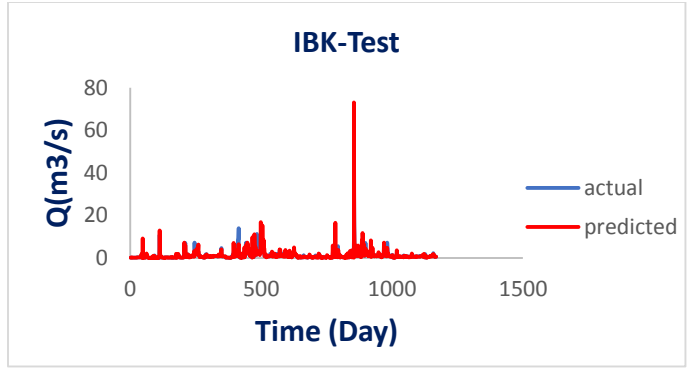
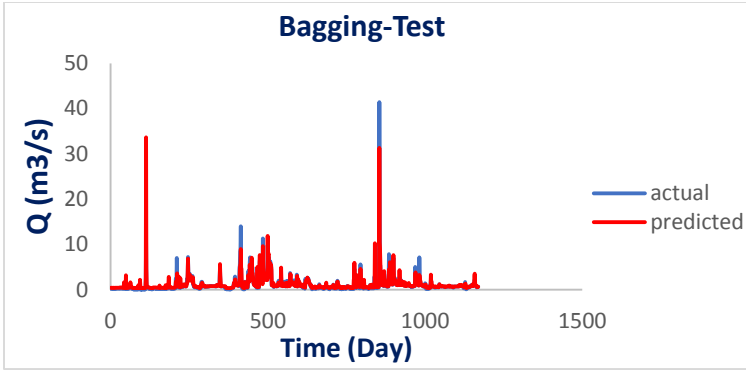
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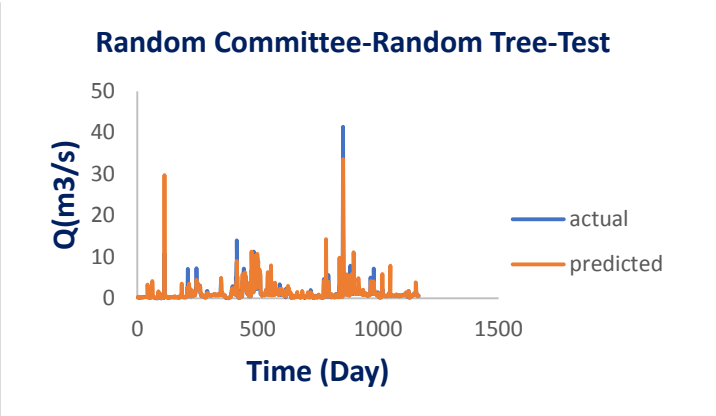
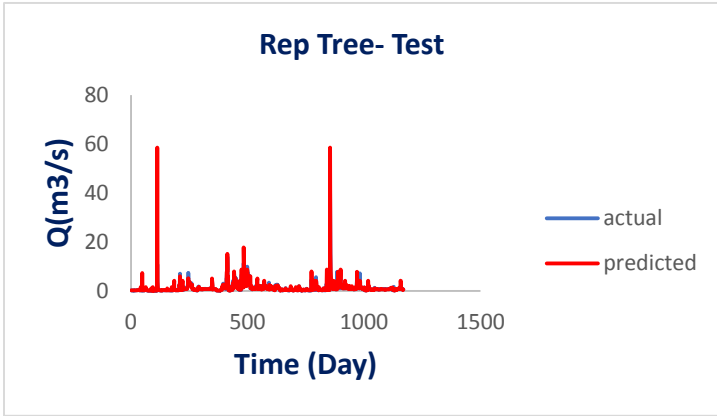
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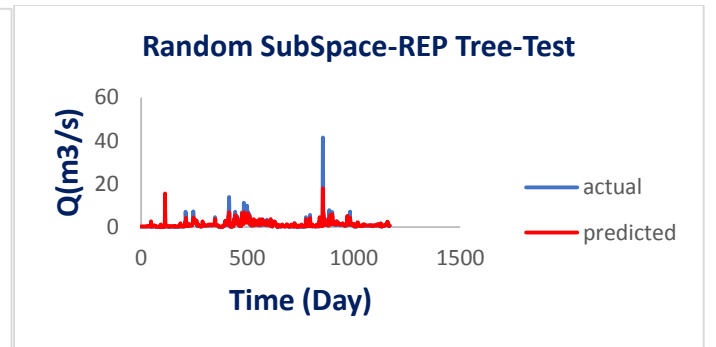
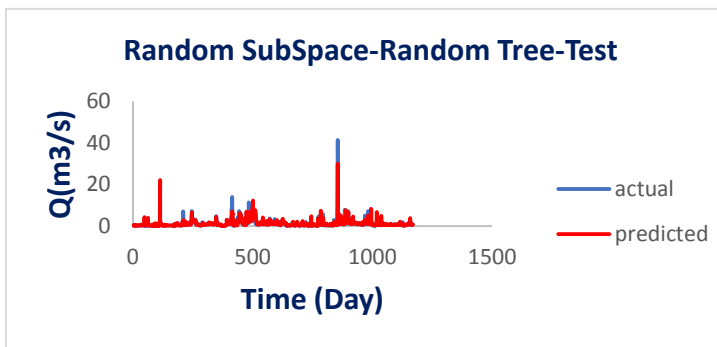
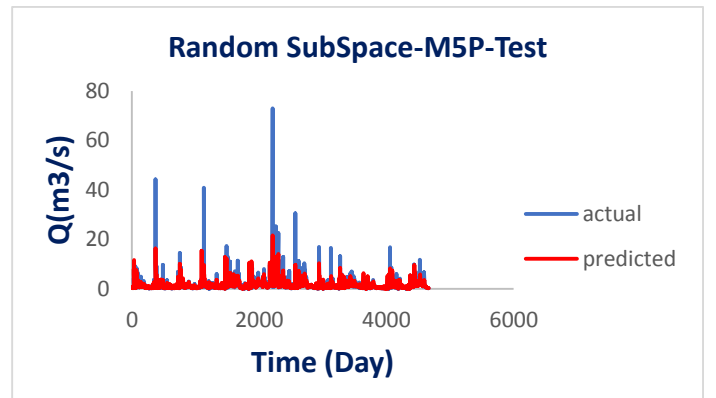
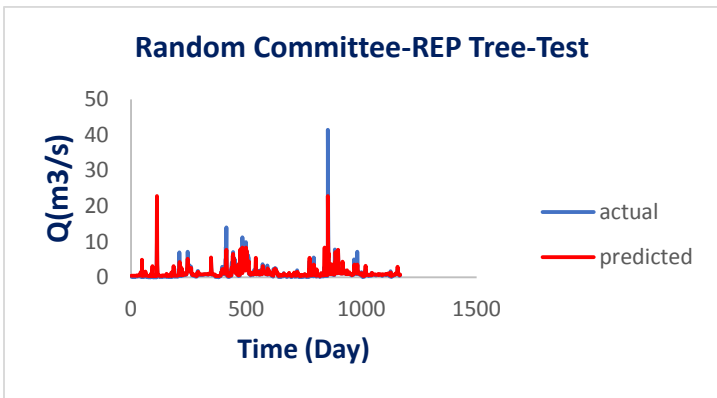
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Fig 1. Location of the Kurkursar River



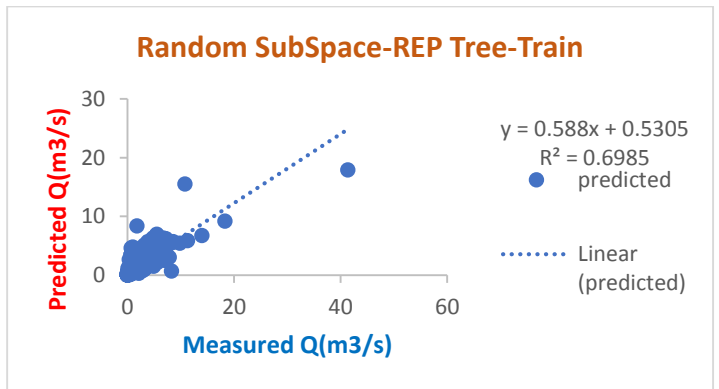
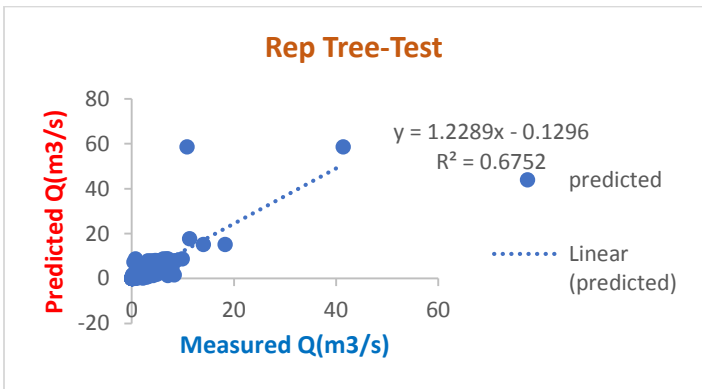
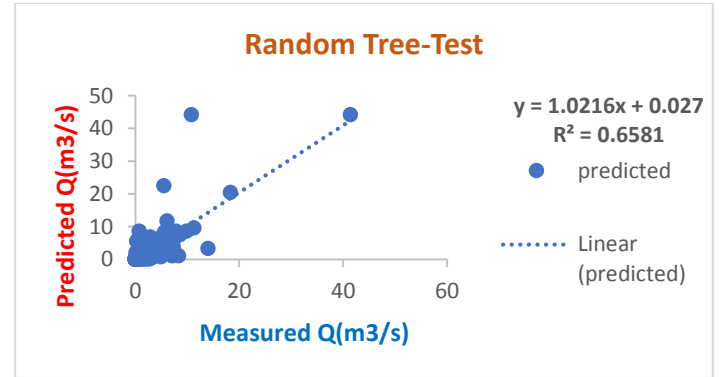
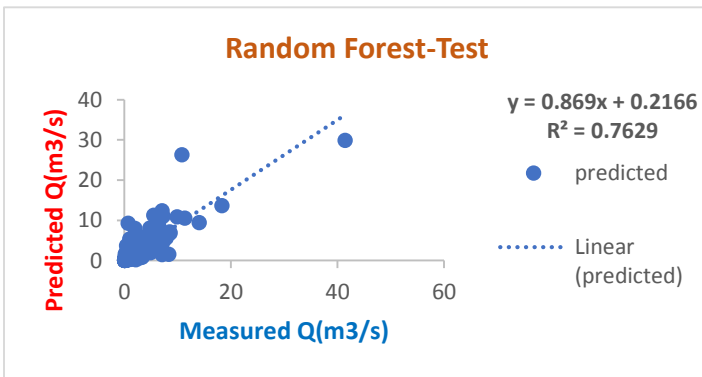
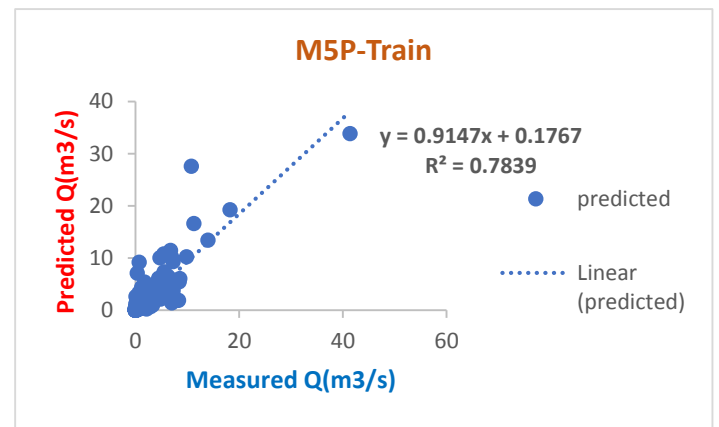
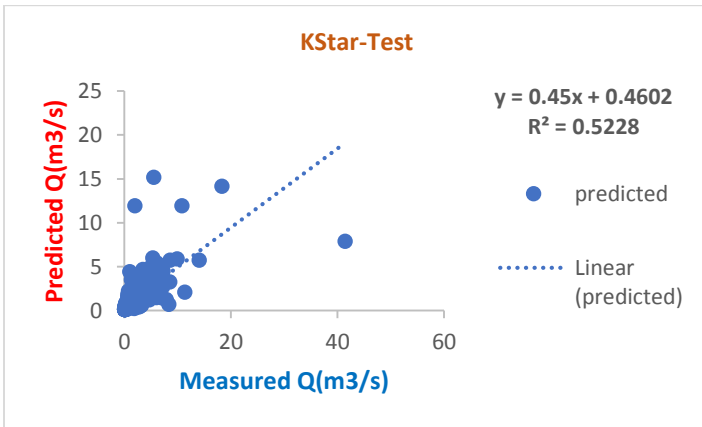
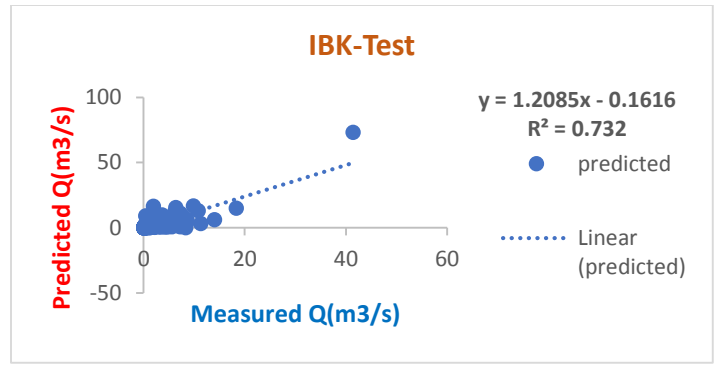
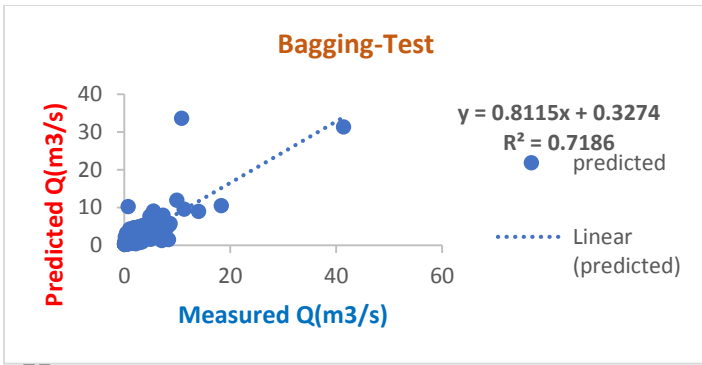


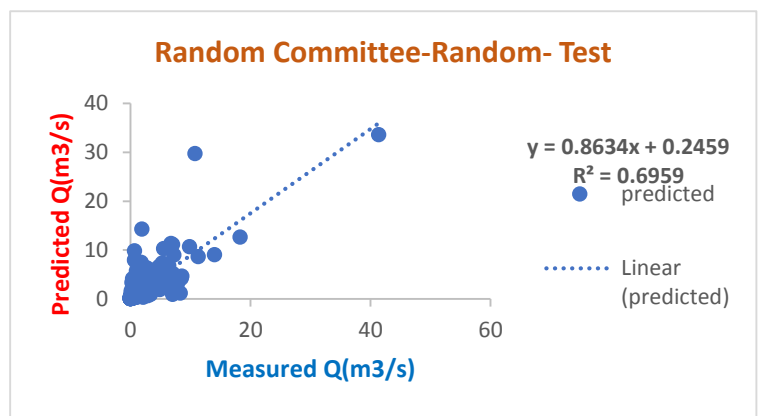
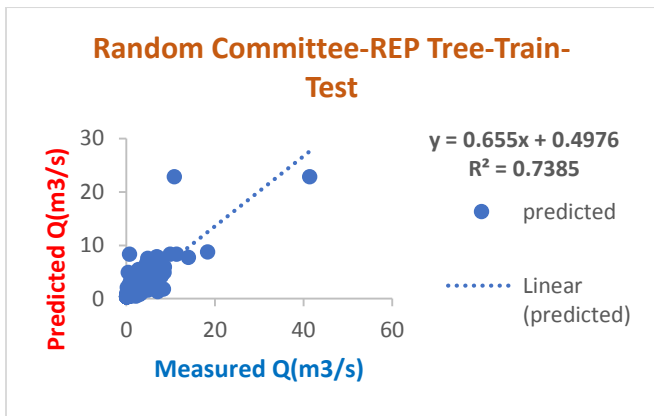
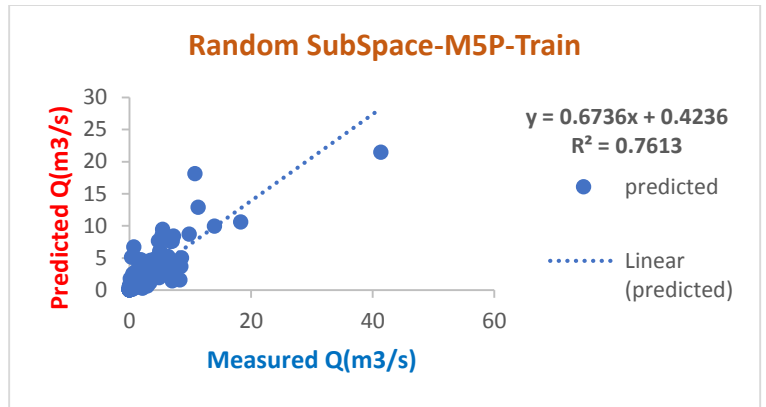
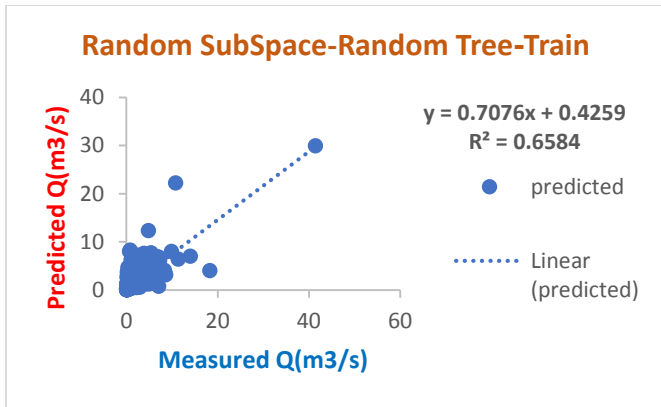
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19 **Fig 2.** Time variation graphs for the predicted and observed values (testing phase)

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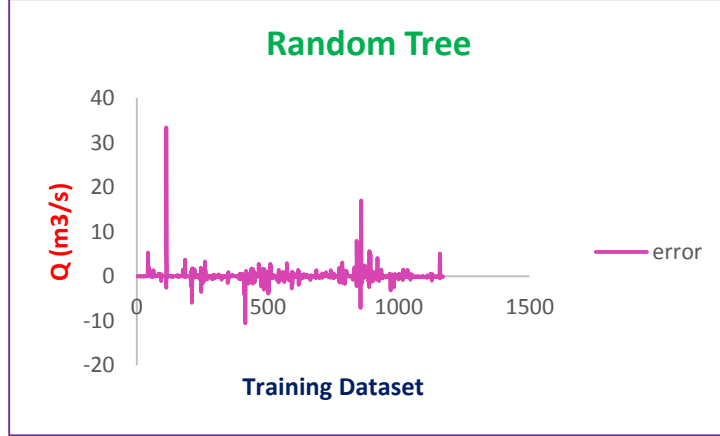
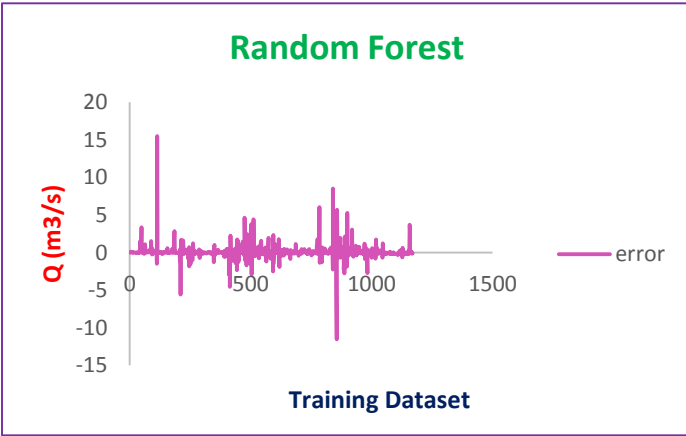
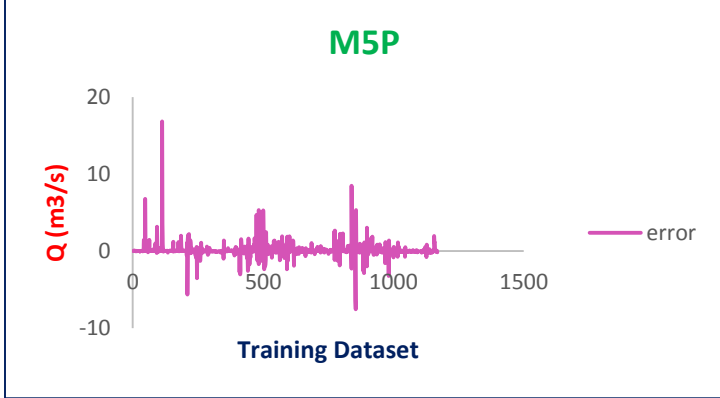
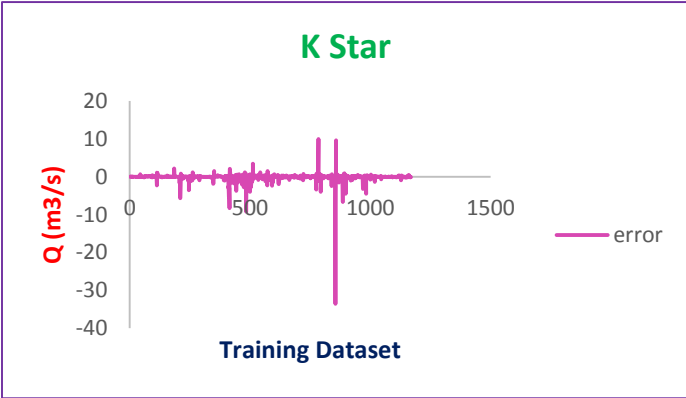
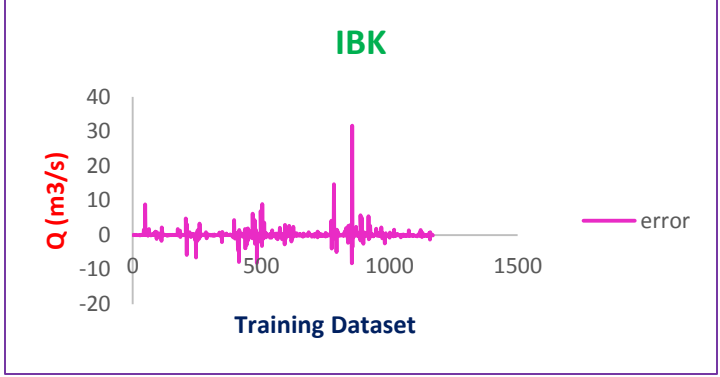
27 **Fig 3.** Scatter plots for the predicted and observed values (testing phase)

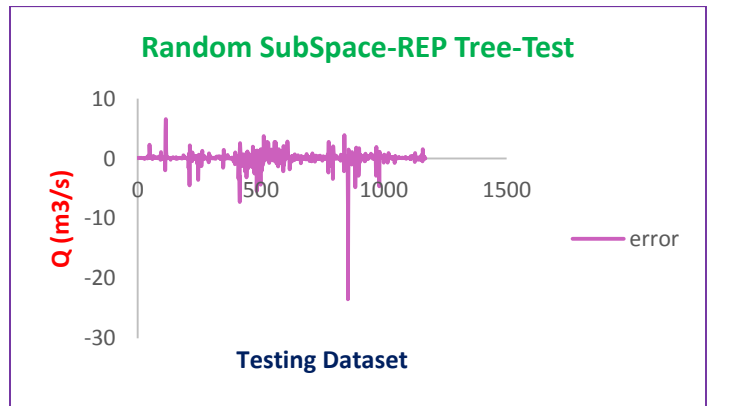
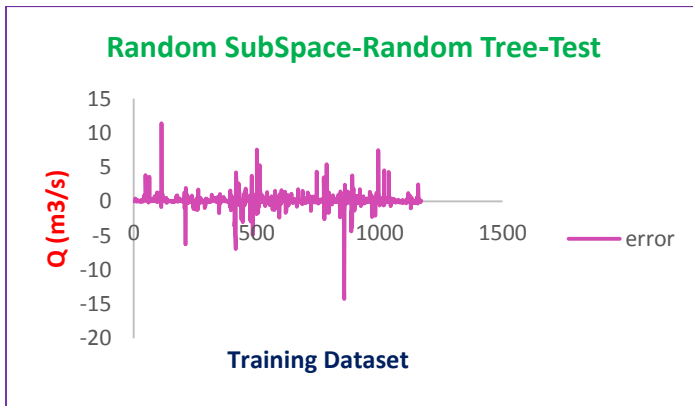
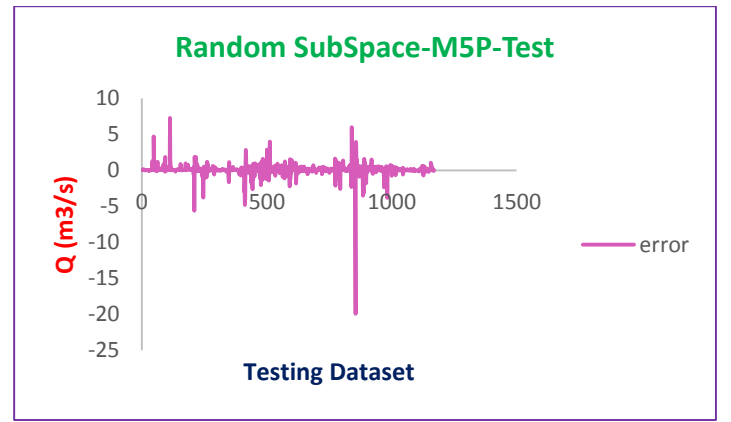
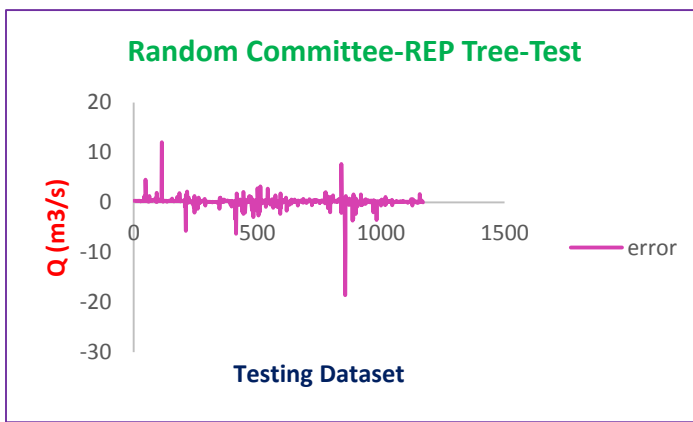
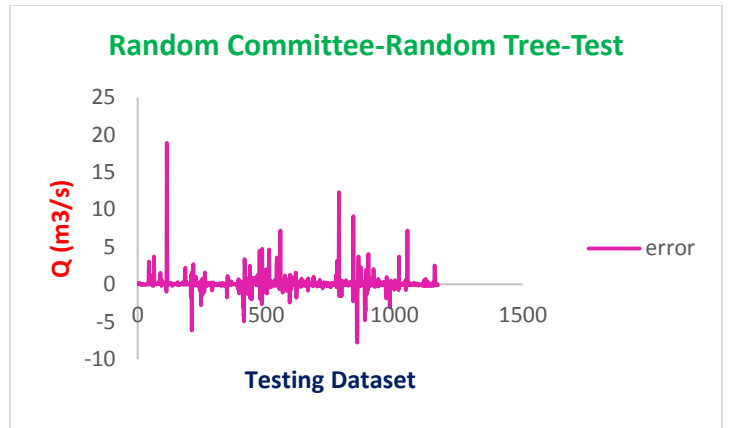
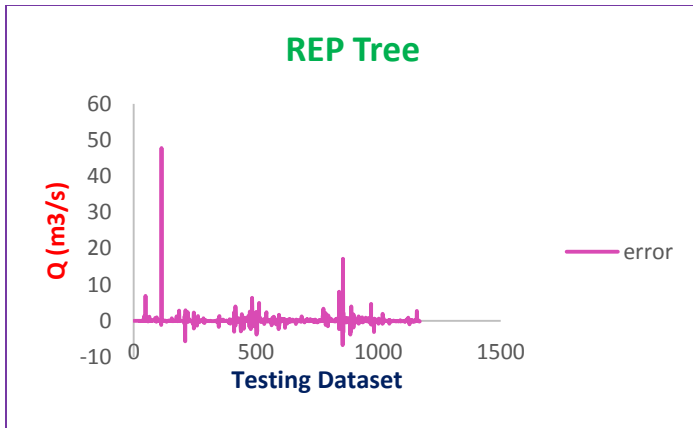
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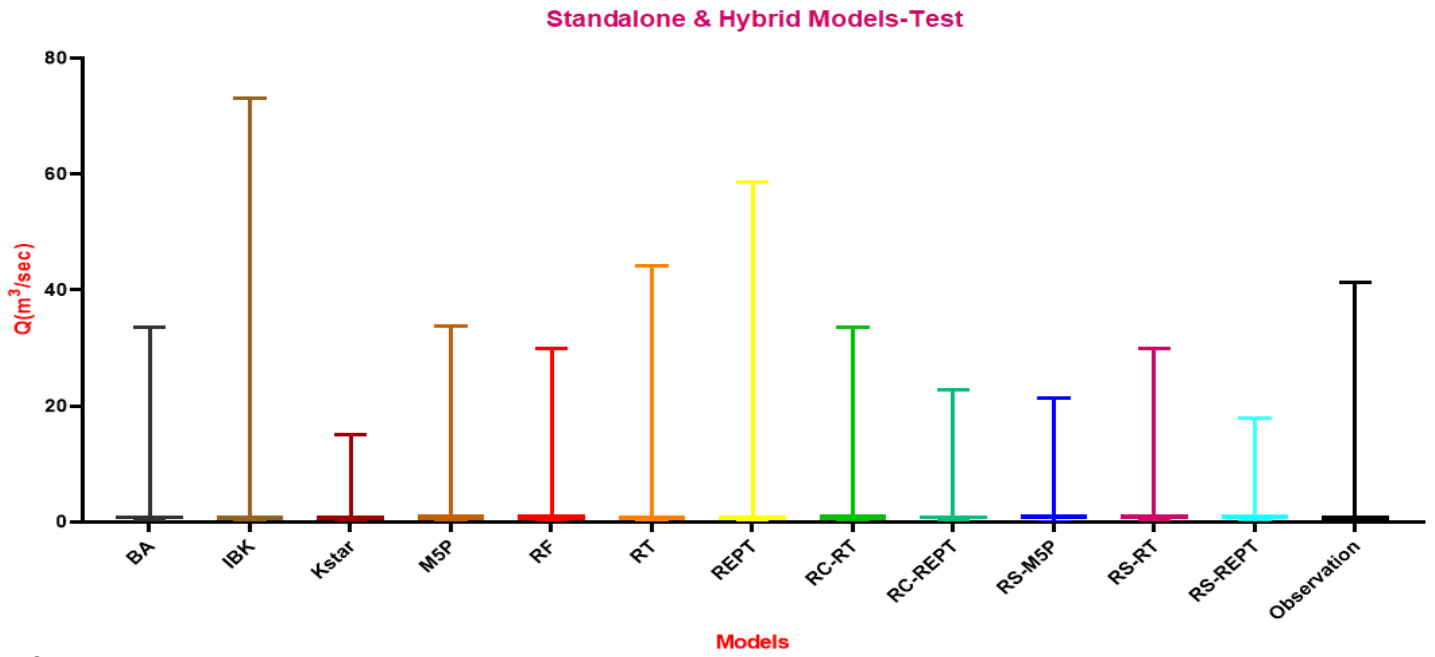
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38 **Fig 4.** Error graphs for the predicted and observed values (testing phase)

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Fig 5. Box plots for determining the best performance with the applied algorithms

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Table 1. Performance indicators for streamflow prediction

Factor	Equation	Factor role	Ref	Range	Performance
R²	$R^2 = 1 - \left(\frac{\sum_{i=1}^{i=N} (Q_t^{ob} - Q_t^{pr})^2}{\sum_{i=1}^{i=N} (Q_t^{ob})^2} \right)$	To show the accuracy of prediction	(Faizollahzadeh Ardabili et al., 2018)	$0.7 \leq R^2 \leq 0.1$	Very good
				$0.6 \leq R^2 \leq 0.7$	Good
				$0.5 \leq R^2 \leq 0.6$	Satisfactory
				$0 \leq R^2 \leq 0.5$	Unsatisfactory
RMSE	$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{i=N} (Q_t^{pr} - Q_t^{ob})^2}$	To show accuracy	(Faizollahzadeh Ardabili et al., 2018)	-	The lower value is better
MAE	$MAE = \frac{1}{N} \sum_{i=1}^{i=N} (Q_t^{pr} - Q_t^{ob})^2$	To show accuracy	(Faizollahzadeh Ardabili et al., 2018)	-	The lower value is better
NSE	$NSE = 1 - \frac{\sum_{i=1}^{i=N} (Q_t^{pr} - Q_t^{ob})^2}{\sum_{i=1}^N (Q_t^{pr} - \overline{Q_t^{pr}})^2}$	Predictive power classification	(Moriasi et al., 2007)	$0.75 < NSE \leq 1.00$	Very good
				$0.65 < NSE \leq 0.75$	Good
				$0.50 < NSE \leq 0.65$	Satisfactory
				$0.4 < NSE \leq 0.50$	Acceptable
				$NSE \leq 0.4$	Unsatisfactory
PBIAS	$PBIAS = \frac{\sum_{i=1}^{i=N} (Q_t^{pr} - Q_t^{ob})}{\sum_{i=1}^{i=N} Q_t^{pr}}$	Predictive power classification	(Legates & McCabe Jr, 1999)	$PBIAS < \pm 10\%$	Very good
				$\pm 10\% \leq PBIAS < \pm 15\%$	Good
				$\pm 15\% \leq PBIAS < \pm 25\%$	Satisfactory
				$PBIAS \geq \pm 25\%$	Unsatisfactory
RSR	$PSR = \sqrt{\frac{\sum_{i=1}^{i=N} (Q_t^{pr} - Q_t^{ob})^2}{\sum_{i=1}^{i=N} (Q_t^{pr} - \overline{Q_t^{pr}})^2}}$	Predictive power classification	(Gupta et al., 1999)	$0 \leq RSR \leq 0.50$	Very good
				$0.50 < RSR \leq 0.60$	Good
				$0.60 < RSR \leq 0.70$	Satisfactory
				$RSR > 0.70$	Unsatisfactory

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Table 2. Statistical parameters for train and test phases

Dataset		R	Q
Min	Train	0	0.002
	Test	0	0.004
Max	Train	149	73.1
	Test	147	41.4
Mean	Train	3.415	1.298
	Test	3.626	1.115
StdDEV	Train	11.165	2.168
	Test	11.451	1.893

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Table 3. Correlation coefficient (CC) between input and output variables

Output variable	Input variable											
	R(t)	R(t-1)	R(t-2)	R(t-3)	R(t-4)	R(t-5)	R(t-6)	Q(t-1)	Q(t-2)	Q(t-3)	Q(t-4)	Q(t-5)
Q(t)	0.563	0.281	0.124	0.0705	0.0681	0.0552	0.0612	0.463	0.297	0.251	0.225	0.211

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Table 4. Input variable combinations

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Model Number	Input variables
1	R(t)
2	R(t), Q(t-1)
3	R(t), Q(t-1), Q(t-2)
4	R(t), R(t-1), Q(t-1), Q(t-2)
5	R(t), R(t-1), Q(t-1), Q(t-2), Q(t-3)
6	R(t), R(t-1), Q(t-1), Q(t-2), Q(t-3), Q(t-4)
7	R(t), R(t-1), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5)
8	R(t), R(t-1), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5), Q(t-6)
9	R(t), R(t-1), R(t-2), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5), Q(t-6)
10	R(t), R(t-1), R(t-2), R(t-3), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5), Q(t-6)
11	R(t), R(t-1), R(t-2), R(t-3), R(t-4), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5), Q(t-6)
12	R(t), R(t-1), R(t-2), R(t-3), R(t-4), R(t-5), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5), Q(t-6)
13	R(t), R(t-1), R(t-2), R(t-3), R(t-4), R(t-5), R(t-6), Q(t-1), Q(t-2), Q(t-3), Q(t-4), Q(t-5), Q(t-6)

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Table 5. Selection of the best combinations for the standalone models

Model Number	M5P		RF		RT		REPT		BA		IBk		Kstar	
	Train	Test	Train	Test	Train	Test	Train	Test	Train	Test	Train	Test	Train	Test
1	1.7055	1.4074	1.4122	1.7606	1.3493	1.9132	1.5542	1.9707	1.6407	1.4364	1.3516		2.0358	1.7237
2	1.273	0.9264	0.6052	0.0972	0.2677	2.3232	1.0479	1.6731	1.1659	1.1659	0.2771	1.9515	1.6562	1.4353
3	1.254	1.2038	0.5721	0.9549	0.1119	2.4254	1.0201	1.6622	1.1573	1.033	0.1362	1.6317	1.2157	1.3859
4	1.2117	1.2390	0.5603	0.9520	0.0897	1.3945	1.0334	1.0334	1.1451	1.0314	0.2118	1.4402	1.9932	1.3323
5	1.2258	1.2702	0.5551	1.0015	0.0832	1.7810	0.9853	1.7262	1.1259	1.0546	0.3725	1.448	0.6121	1.3295
6	1.2007	1.2855	0.5489	0.9687	0.0727	1.5968	0.985	1.7317	1.1359	1.0782	0.3699	1.4619	0.3553	1.3312
7	1.1911	1.0980	0.5579	0.9695	0.0604	1.8760	0.9813	1.7334	1.140	1.0702	0.3673	1.4438	0.2053	1.3651
8	1.1851	1.0456	0.5510	0.9582	0.0521	1.7433	1.1029	1.7553	1.1368	1.073	0.3671	1.4664	0.1284	1.426
9	1.1612	1.1476	0.5486	0.9591	0.0528	1.1808	1.1027	1.7551	1.1332	1.0754	0.3685	2.1	0.1074	1.5069
10	1.1613	1.1311	0.5778	1.011	0.0586	1.4305	1.0922	1.7686	1.1326	1.0752	0.3686	2.1028	0.0833	1.5061
11	1.1598	1.1333	0.5667	0.9915	0.0475	1.7151	1.0922	1.7686	1.1327	1.0854	0.3668	2.0952	0.0748	1.5251
12	1.1557	1.1375	0.5679	1.0101	0.0459	1.6121	1.0922	1.7686	1.1299	1.0851	0.3719	2.1039	0.0664	1.5302
13	1.1378	1.1931	0.5650	1.033	0.0458	1.6121	1.0922	1.7686	1.1306	1.0852	0.3653	2.1001	0.0545	1.5379

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Table 6. R^2 coefficient for standalone and hybrid models

Model Number	Models	Train	Test
1	BA	0.5485	0.7186
2	M5P	0.6586	0.7839
3	RF	0.9431	0.7629
4	RT	0.9983	0.6581
5	REPT	0.7728	0.6752
6	IBK	0.9905	0.732
7	K Star	0.9398	0.5228
8	RC-RF	0.9497	0.7347
9	RC-RT	0.9997	0.6959
10	RC-REPT	0.7171	0.7385
11	RS-M5P	0.6759	0.7613
12	RS-RT	0.9984	0.6584
13	RS-REPT	0.6027	0.6985

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Table 7. Results of the evaluation criteria for standalone and hybrid models (testing phase)

		RMSE	MAE	NSE	PBIAS	PSR
Bagging	Train	1.0685	0.327892	0.701855	-2.968	0.54603
	Test	0.51615	0.092012	0.746796	-10.511	0.50319
IBK	Train	0.21177	0.028575	0.969183	-0.3674	0.17555
	Test	1.17545	0.291303	0.506284	-6.3558	0.70265
K Star	Train	0.61199	0.146363	0.742641	5.27741	0.50731
	Test	1.08512	0.230033	0.579253	13.7364	0.64865
M5P	Train	1.27287	0.35674	-0.11331	0.14091	1.05514
	Test	0.75604	0.215459	0.79575	-7.3175	0.45194
RF	Train	0.56023	0.156762	0.784338	-0.1269	0.4644
	Test	0.77696	0.22041	0.784294	-6.3254	0.46444
RT	Train	0.08982	0.103748	0.994456	-0.0007	0.07446
	Test	1.13815	0.263821	0.53712	-4.5818	0.68035
REPT	Train	1.03332	0.328143	0.266305	0.00898	0.85656
	Test	1.36649	0.245161	0.33276	-11.274	0.81685
RS-REPT	Train	1.44856	0.412903	-0.44184	-0.0008	1.20077
	Test	0.87401	0.264426	0.727041	-6.3691	0.52245
RS-RT	Train	0.0867	0.029795	0.994835	0.00025	0.07187
	Test	0.91089	0.304613	0.703517	-8.9486	0.5445
RS-M5P	Train	1.31697	0.361223	-0.19179	0.24102	1.09169
	Test	0.77176	0.228345	0.787172	-5.3465	0.46133
RC-REPT	Train	1.31823	0.407127	-0.19407	-0.0021	1.09274
	Test	0.80897	0.271162	0.76615	-10.123	0.48358
RC-RT	Train	0.03642	0.021295	0.999088	0.00033	0.03019
	Test	0.90939	0.248427	0.704491	-8.3911	0.54361
RC-RF	Train	0.55407	0.159346	0.789053	0.33768	0.45929
	Test	0.88352	0.324295	0.74151	-3.5204	0.50842

Table 8: Optimum values for models parameters

Parameter	Optimum value										
	BA	IBK	K STAR	M5P	RF	RT	REPT	RC-RT	RS-M5P	RS-REPT	RC-RF
Bag size percentage	100	-	-	-	100	100	-	-	-	-	-
Batch size	100	100	-	-	100	100	100	100	100	100	100
Num decimal places	2	2	2	2	2	2	2	2	2	2	2
Num execution slots	1	-	-	-	1	-	-	1	1	1	1
Num iteration	10	-	-	-	100	-	-	10	10	10	10
Seeds	1	-	-	-	1	1	-	1	1	1	-
Min num instances	-	-	-	4	-	2	2	-	-	-	-
Build regression tree	-	-	-	False	-	-	-	-	-	-	-
Do not check capabilities	-	False	False	False	-	-	False	False	-	-	False
Debug	-	False	False	False	False	False	False	False	False	False	False
Unpruned	-	-	-	False	-	-	False	-	-	-	-
Use unsmoothed	-	-	-	False	-	-	-	-	-	-	-
Max depth	-	-	-	-	0	0	-1	-	-	-	-
Num feathers	-	-	-	-	-	-	-	-	-	-	-
K value	-	-	0	-	-	0	-	-	-	-	-
Min variance Prop	-	-	-	-	-	-	0.001	-	-	-	-
Num folds	-	-	-	-	-	0	-	-	-	-	-
Global blend	-	-	20	-	-	-	-	-	-	-	-
Entropic auto blend	-	-	False	-	-	-	-	-	-	-	-
Missing mode	-	-	Average column entropy curve	-	-	-	-	-	-	-	-
KNN	-	1	-	-	-	-	-	-	-	-	-
Cross-validation	-	False	-	-	-	-	-	-	-	-	-
Distance weighting	-	No	-	-	-	-	-	-	-	-	-
Subspace size	-	-	-	-	-	-	-	-	0.5	0.5	-
Number of fold	-	-	-	-	-	-	3	-	-	-	-